### Today's lesson is on Simplifying Expressions.

Gather these materials:

Clicker

Notebook

Pen

Get ready for the warm-up questions



# A mathematical phrase with at least one variable is called an

Text in the word that correctly completes the sentence.



### Solve 2c + t for c = 1/2 and t = 5

Text in your number answer.

## **Simplifying Expressions**

### What You'll Learn

To simplify algebraic expressions using properties of operations

New Vocabulary like terms, coefficient

### Why Learn This?

You evaluate algebraic expressions by substituting values for variables. Scientists  $often \, substitute \, data \, from \, experiments \, into \,$ formulas with several variables to interpret



Like terms are terms that have the same variable factors. For example,

12x and 3x are like terms, but 4a and 5b are not like terms. You can use the properties of operations to order, group, and combine like terms.

A coefficient is a numerical factor of a term with a variable. In each of the terms below, the coefficients are highlighted.

Coefficients -



1 EXAMPLE Combine like terms in the expression

$$8p+13p+p.$$

$$8p + 13p + p = 8p + 13p + 1p$$

Rewrite p as 1p.

$$= (8 + 13 + 1)p$$

Distributive Property

← Combine like terms by adding.

### **EXAMPLE** Using Properties to Add and Subtract



**1** Simplify 5x + 9 + 2x - 4.

5x + 9 + 2x - 4  $\leftarrow$  Identify which parts of the expression are like terms.

 $= 5 x + 2 x + 9 - 4 \quad \leftarrow \text{Commutative Property of Addition}$ 

 $= (5+2)x + 9 - 4 \leftarrow Distributive Property$ 

 $= 7x + 9 - 4 \qquad \leftarrow$  Simplify the coefficient. = 7x + 5

= 7x + 5 $\leftarrow$  Simplify.

The simplified expression is 7x + 5.



## 🕉 Quick Check

Simplify each expression.

**a.** 
$$2x + 8 + 4x - 5$$

### Simplify:

$$10r - 5 + 3 + r$$



## Simplify k - 2 + 7 - 9k



 $\bigcirc$  10k + 9



-8k + 5



-10k -5



D -8k -5

Sometimes an expression should be expanded before it is simplified.

### **EXAMPLE** Expanding Expressions

Simplify  $\frac{2}{3}(12y + 9) + 4$ .

$$\frac{2}{3}(12y+9)+4$$

 $= (8y + 6) + 4 \qquad \leftarrow \text{Distributive Property}$   $= 8y + (6 + 4) \qquad \leftarrow \text{Associative Property of Addition}$   $= 8y + 10 \qquad \leftarrow \text{Simplify}$ 

The simplified expression is 8y + 10.

### Simplify:

$$9 - 4(3z + 2)$$



2. Simplify each expression.

a. 
$$6(2x+3)-4$$



Simplify: 8 - 2(6s + 1)



36s + 9



-12s + 9



6 - 12s



-36s + 9

You can use the Distributive Property to rewrite an addition expression as a product of two factors. This process is called factoring. Use the greatest common factor (GCF) so the expression is factored completely.

### EXAMPLE

### **Factoring Expressions**

0

a. Factor 4x + 14.

GCF of 4 and 14 is 2.  $\leftarrow$  Identify the GCF.  $4x + 14 = 2 \cdot 2x + 2 \cdot 7 \leftarrow$  Factor each term by the GCF.

= 2(2x + 7)  $\leftarrow$  Distributive Property

The factored expression is 2(2x + 7).

**b.** Factor 12y - 6

GCF of 12 and 6 is 6.  $\leftarrow$  Identify the GCF.

 $12y - 6 = 6 \cdot 2y - 6 \cdot 1$   $\leftarrow$  Factor each term by the GCF. = 6(2y - 1)  $\leftarrow$  Distributive Property

The factored expression is 6(2y - 1).

**3** Factoring Expressions Factor 21x + 35.

GCF of 21 and 35 is 7.

 $\leftarrow$  Identify the GCF.

$$21x + 35 = 7 \cdot \boxed{3x} + 7 \cdot \boxed{5}$$
.  $\leftarrow$  Factor each term by the GCF.

$$=7\left(\boxed{3x} + \boxed{5}\right)$$
  $\leftarrow$  Distributive Property

The factored expression is 7(3x + 5).

## **Ø** Quick Check

3. Factor each expression completely.

a. 
$$9x + 15$$



**Factor each expression completely:** 

$$36 + 24t$$

# Factor the expression completely: 18 - 24m



(A) 9(2 - 2m)



6(3 - 4m)



4(4 - 6m)



(D) 6(3 - 8m)

### Check Your Understanding

1. **Vocabulary** Terms that have the same variable factors, such as 7y and -3y, are called  $\frac{?}{}$ .



### **Extra practice**

Simplify each expression.

3. 
$$8n - 2n$$

4. 
$$30s + 7 + 3s$$

5 
$$6 - 3r - 3$$

$$3.2v + 4 + 0.5$$

5. 
$$6 - 3r - 3$$
 6.  $2y + 4 + 0.5$  7.  $2(15 + 5w) -$ 

### extra practice

Identify the greatest common factor of the terms in each expression.

8. 4n - 40

9. 27 + 18v

**10.** 15t + 25

# Power down your clickers and put them away.

You have an assignment worksheet.

Simplify each expr		2 0	2 10	2 2 . 0	
1. $12 - \frac{1}{3}m + 4$	- 4m 2. a - z + 1	2. a - 2 + 13 + 8a		3. 10q - 2q + 3 - 9	
<b>4.</b> $8 - g - 2 + 5g$	<b>5.</b> 2.2k + 5	+7.9k + 8	64	r - 2r - 6 - 4	
7. 0.2(15 - 3t) -	1.8 <b>8.</b> 7x - 5(3x	8. $7x - 5(3x + 12)$		9. $\frac{1}{3}(9z-27)+12$	
Factor each expres	sion completely.				
<b>10.</b> 42 <i>r</i> - 18	<b>11.</b> 100 - 50d	<b>12.</b> 24 <i>x</i> +	- 64	<b>13.</b> $-9y - 39$	
<b>14.</b> 60 – 24 <i>x</i>	<b>15.</b> 9w – 81	16. 132 -	- 77t	<b>17.</b> 16 <i>y</i> – 56	
Use >, <, or = to	make each statement true.				
	$4p + 2 \cdot 4 - 3p$				
	6 + 2(m + n) - 11 $2 \bigcirc 3(5 - x) + 2x$				
	eter of a rectangle with len				